



## On modeling global solar irradiation using air temperature for Alagoas State, Northeastern Brazil



Cícero Manoel Dos Santos<sup>a</sup>, José Leonaldo De Souza<sup>a, \*</sup>, Ricardo Araujo Ferreira Junior<sup>a</sup>, Chigueru Tiba<sup>b</sup>, Rinaldo Oliveira de Melo<sup>b</sup>, Gustavo Bastos Lyra<sup>c</sup>, Iêdo Teodoro<sup>a</sup>, Guilherme Bastos Lyra<sup>a</sup>, Marco Antonio Maringolo Lemes<sup>a</sup>

<sup>a</sup> Laboratório de Agrometeorologia e Radiometria Solar, Instituto de Ciências Atmosféricas, Universidade Federal de Alagoas, Campus A.C. Simões, BR 104-Norte, Km 97, Tabuleiro dos Martins, CEP 57072-970 Maceió, Alagoas, Brazil

<sup>b</sup> Departamento de Energia Nuclear da Universidade Federal de Pernambuco, Av. Prof. Luiz Freire, 1000-CDU, CEP 50.740-540 Recife, Pernambuco, Brazil

<sup>c</sup> Departamento de Ciências Ambientais, Instituto de Florestas, Universidade Federal Rural do Rio de Janeiro, Rod. BR 465, Km 7, CEP 23890-970 Seropédica, Rio de Janeiro, Brazil

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### ABSTRACT

The present study assesses the performance of nine empirical models: the models of Bristow & Campbell and Hargreaves & Samani (together with their modified versions) in estimating the daily and monthly solar irradiation using just extraterrestrial solar irradiation and air temperature extremes (maximum and minimum) as input data. Two schemes to calculate the air temperature amplitudes ( $\Delta T_1$  and  $\Delta T_2$ ) were used. The data used in this study cover the period from 2007 to 2009 and were collected at eight solarimetric stations in Alagoas State (Northeastern Brazil); three are located in the interior, two in the hinterlands and three in the humid/coastal zones. Statistical parameters were used to evaluate the model performance. The estimates obtained with the  $\Delta T_1$  scheme are better than those using the  $\Delta T_2$  scheme for the interior (1.10%) and hinterlands (2.50%). The daily (0.160–0.201) and monthly (0.158–0.199) values of the coefficients of the original Hargreaves and Samani model did not show significant differences among them; this was not the case of Bristow and Campbell model. Have a special from the coastline (thermal amplitude, humidity and cloudiness) and altitude (bulk thermal capacity and optical depth of the atmosphere). On the daily basis, the original model of Hargreaves & Samani yields better estimates than those obtained with the Bristow & Campbell model: 2.30% (interior) and 5.20% (hinterlands). The latter had a better performance mainly for the sites along the humid/coastal zone (10.20%).

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### 1. Introduction

The global solar irradiance ( $R_g$ ), although considered an important variable in many areas of human activities (e.g. agriculture, climatology and renewable energy), is not measured with an adequate space and time resolution due to the maintenance cost and the frequent calibration procedures of the instruments [1,33]. Indeed, the number of weather stations that measure  $R_g$  on an operational basis is quite small when compared to that of meteorological stations. For instance, among the 3731 surface stations in Spain only 200 measure the sunlight duration and from these, mere 56 include measurements of  $R_g$  [2]. Only 69 surface meteorological stations in India out of a total of 194 monitor the global solar

irradiance [34]. Measurements of  $R_g$  in Brazil, even with the present network consisting of 523 automatic stations operated by the National Institute of Meteorology, are insufficient due to the continental size of the country. Therefore the number of empirical models that have been developed to overcome the scarcity of  $R_g$  measurements is not surprising. These models estimate global solar irradiation ( $H_g$ ) – the integral of  $R_g$  – on an hourly [3], daily [4], monthly [5] and annual [6] bases quite satisfactory. The most sophisticated models use several types of meteorological variables (e.g. relative humidity, precipitation, water vapor pressure and air temperature) as input data. Most empirical models are based on Ångström [7] who found a linear relation between the daily averaged  $H_g$  (normalized by the extraterrestrial solar irradiation,  $H_0$ ) and the sunlight duration (ratio of the sunshine period and the daytime length) [35].

Bristow & Campbell [8], while searching for an empirical relation between air temperature and global solar irradiation, suggested a

\* Corresponding author. Tel.: +55 82 32141360; fax: +55 82 32141367.  
E-mail address: [jsl@ccen.ufal.br](mailto:jsl@ccen.ufal.br) (J.L. De Souza).

relation between  $H_g/H_0$  and the maximum and minimum air temperature differences for three localities in the USA. This model has since been modified by many authors. Meza & Varas [9] adjusted the model for different locations in Chile by keeping the coefficients  $\beta_1$  (=0.75) and  $\beta_3$  (=2.0) constant, while  $\beta_2$  was free to change as part of the model calibration. Donatelli & Campbell [10] modified the original model of Bristow & Campbell by adding the monthly mean of the thermal amplitude ( $\Delta T_m$ ). Weiss et al. [11] included  $H_0$ , but kept  $\beta_1$  (=0.75) and  $\beta_3$  (=2.0) fixed, just as done by Meza & Varas, with  $\beta_2$  playing the role of a free parameter. Abraha & Savage [12] adjusted the same model by keeping the coefficients  $\beta_1$  (=0.75) and  $\beta_3$  (=2.0) constant and inserting the monthly mean thermal amplitude ( $\Delta T_m$ ) into the exponential; their coefficient  $\beta_2$  is determined by calibration procedures. Assuming that the difference between the daily maximum and minimum air temperatures gives general information on the cloudiness, Hargreaves & Samani [13] proposed to estimate  $H_g$  as a function of  $H_0$  and the air temperature difference. Annandale et al. [14] introduced the altitude factor for nine sites in North America in a multiplicative form following Allen's [15] suggestion. Hargreaves et al. [16] modified the Hargreaves & Samani model aiming to improve its performance by keeping two coefficients ( $\beta_1$  and  $\beta_2$ ) in an additive) and multiplicative forms. Hunt et al. [17] proposed a modification in the model of Hargreaves & Samani by inserting the coefficient  $\beta_2$  additively.

The main objectives of this work are: 1 – to assess the performance of two methods using thermal amplitudes in their adjustment, 2 – to determine the coefficients of their nine empirical models (using air temperature as input data) for  $H_g$  at eight sites in Alagoas State, on a daily and monthly bases and 3 - to assess the performance of each model.

## 2. Sites and measurements

### 2.1. Sites and data

The study uses meteorological data collected at eight automatic stations located in different climate regions within the Alagoas State, Northeastern Brazil: a) interior (Água Branca, Pão de Açúcar and Santana do Ipanema), b) hinterlands (Arapiraca and Palmeira dos Índios) and c) humid/coastal zones (Maceió, Coruripe and São José da Laje). Table 1 and Fig. 1 show their geographical positions together with the average annual precipitation and temperature.

The  $H_g$  measurements were made with a black and white Eppley pyranometer [measurement band: 285–2800 nm and cosine response:  $\pm 2.0\%$  ( $0^\circ < \Theta_z < 70^\circ$ )], where,  $\Theta_z$  is the zenith angle. The maximum and minimum air temperatures were measured using a HMP45C Väissällä Inc. sensor [measurement band:  $-40^\circ\text{C}$  to  $+60^\circ\text{C}$  (accuracy:  $\pm 0.20^\circ\text{C}$ );  $20^\circ\text{C}$  to a  $40^\circ\text{C}$  (accuracy:  $\pm 0.50^\circ\text{C}$ )]. The sensors used in the field experiments had been purchased just before the beginning of the measurements (September, 2007) and were frequently calibrated using the Eppley

Precision Spectral Pyranometer throughout the experiment duration. The end of the measurements stage was December, 2009. The radiometers were installed on a 10-m high tower, with no obstacles around and were connected to a data acquisition system (CR100, Campbell Scientific, Utah, USA), programmed to make measurements every five seconds and store the averages every minute.

### 2.2. Definitions

According to Paulescu et al. [18] the empirical models used to estimate  $H_g$  with meteorological data, may be classified into two distinct classes. The first class consists of models that make use of air temperature and other meteorological variables (precipitation and relative humidity e.g. Munner et al. [32]); models of the second class use only air temperature as input data. All the models used in this study belong to the second class and are listed in Table 2, similar to Liu X et al. [19].

### 2.3. Data analysis

The thermal amplitude,  $\Delta T$ , is defined as the difference between the largest and smallest values in the temperature series, and is given by two different methods. They express the air temperature interval,  $\Delta T_1$  [13] and  $\Delta T_2$  [8] using, respectively,

$$\Delta T_1(i) = T_{\max}(i) - T_{\min}(i) \quad (1)$$

$$\Delta T_2(i) = T_{\max}(i) - \frac{[T_{\min}(i) + T_{\min}(i+1)]}{2} \quad (2)$$

where,  $\Delta T_1(i)$  and  $\Delta T_2(i)$  are the diurnal air temperature variations for the  $i$ -th day;  $T_{\max}(i)$  is the maximum air temperature for the  $i$ -th day and  $T_{\min}(i)$  and  $T_{\min}(i+1)$  are the minimum air temperatures for the  $i$ -th and the following day, respectively. The models were validated using both temperature schemes.  $H_0$  was calculated as a function of the local latitude ( $\varphi$ ), solar declination ( $\delta$ ), day ( $d_n$ ), the solar constant ( $S_0 = 1367 \text{ W m}^{-2}$ ) and solar hourly angle ( $\omega$ ) [20]. The models were calibrated using data collected during 2007 and 2008; the data set obtained in 2009 was used only to validate them, by comparing observations and model outputs.

The models were analyzed on a daily and monthly base using two quality control criteria to guarantee data reliability. The filtering used by Ceballos et al. [21] implies: a) the daily averaged irradiation must fall within the interval ( $2.59 \text{ MJ m}^{-2}$ ,  $34.56 \text{ MJ m}^{-2}$ ) and b) the difference between the observed and estimated values in the day must, in absolute value, be less than  $8.64 \text{ MJ m}^{-2}$ . Additionally, it was imposed that the number of pairs of observed and estimated values should not be less than 15 in the month. These criteria eliminated less than 1% of the original data set used in this study. To assess the model performance in terms of  $H_g$ , the MBE (mean bias error) [22], RMSE (root mean square error) [23], correlation coefficients ( $r$ ) and  $t$ -test [23] were used. Some of them are given below:

$$\text{MBE} = \frac{\sum_{i=1}^N (P_i - O_i)}{N} \quad (3)$$

$$\text{RMSE} = \left[ \frac{\sum_{i=1}^N (P_i - O_i)^2}{N} \right]^{\frac{1}{2}} \quad (4)$$

where  $P_i$  and  $O_i$  are the estimated and observed irradiation, respectively.  $N$  is the number of observations. Positive MBE values

**Table 1**

Main characteristics of the observation sites – Lat. = southern latitude in degrees, Long. = western longitudes in degrees, Alt. = altitude in meters,  $\bar{P}$  = annual average precipitation in mm and  $\bar{T}$  = annual average air temperature in ( $^\circ\text{C}$ ).

ID	Site	Lat. (S)	Long. (W)	Alt. (m)	$\bar{P}$ (mm)	$\bar{T}$ ( $^\circ\text{C}$ )
1	Água Branca	9.25	37.93	593.0	1051.4	23.7
2	Pão de Açúcar	9.74	37.43	46.0	571.87	27.6
3	Santana do Ipanema	9.37	37.23	279.4	754.7	26.5
4	Palmeira dos Índios	9.40	36.65	328.0	869.6	25.3
5	Arapiraca	9.70	36.60	239.0	1055.2	24.3
6	Maceió	9.47	35.83	127.0	1817.6	25.4
7	Coruripe	10.02	36.27	108.7	1563.1	26.1
8	São José da Laje	8.97	36.06	344.7	1248.9	24.8

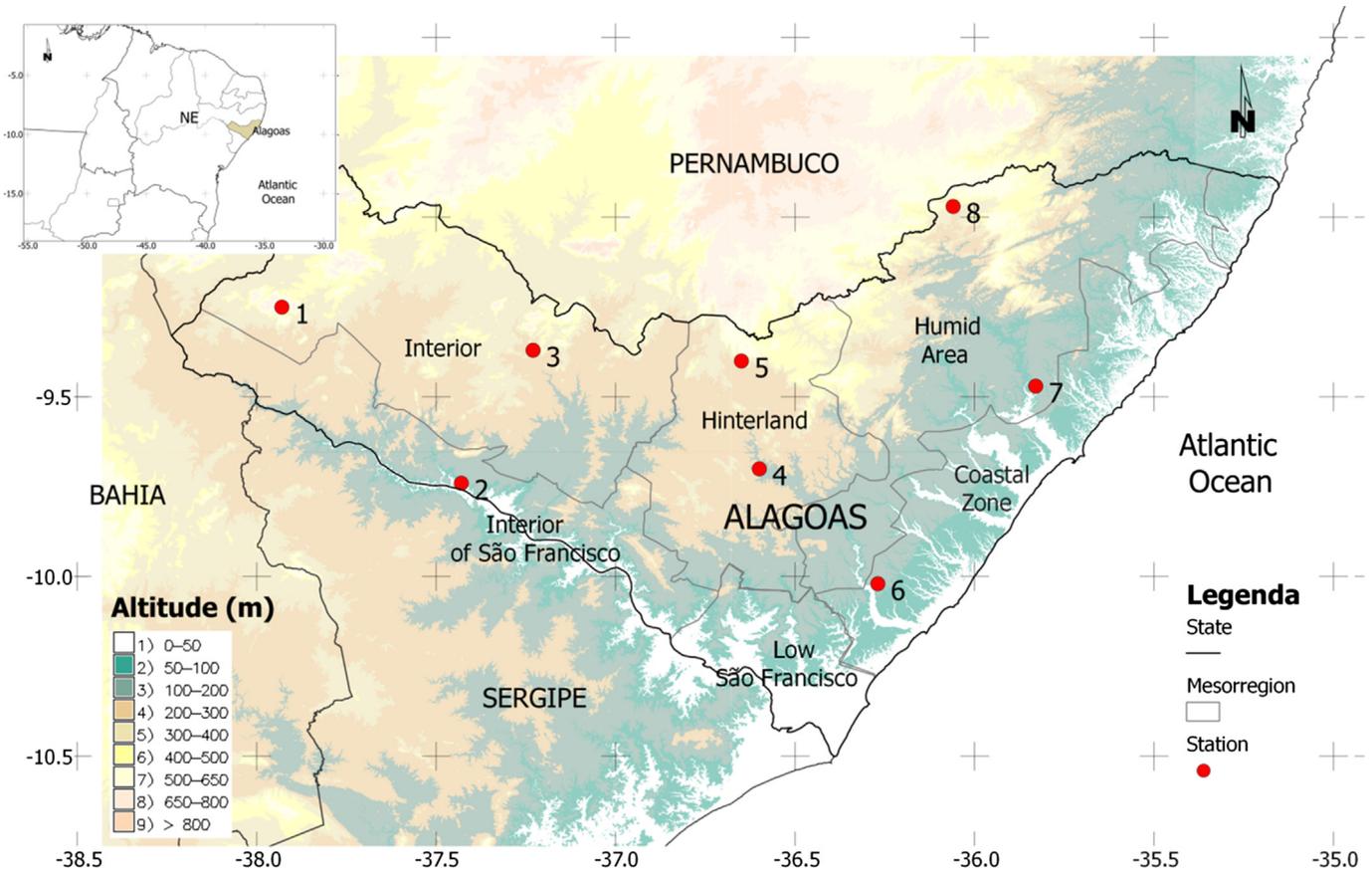


Fig. 1. Location of the solarimetric stations in Alagoas States, Northeastern Brazil.

indicate an overestimate and give long term information on the model performance, associated with systematic errors. The less the absolute value of MBE, the better will be the performance of the tested. RMSE, a non-negative number, gives a short term measure of the spreading of the estimates with respect to the observed data, being always expressed in the same units used in the original data and is associated with random errors. T-test allows model inter-comparison, indicating whether the estimates are or not significant.

### 3. Results and discussions

#### 3.1. Coefficients for the daily global solar irradiation ( $H_g^d$ )

The values of the daily coefficients (Table 3) for the nine models and the eight selected sites of Alagoas, showed little difference

(overall average: 3.7%), regarding the use of  $\Delta T_1$  or  $\Delta T_2$  in agreement with Liu X et al. [19], although the  $\Delta T_1$  scheme may yield a better precision, in particular for high altitudes. The reason for this lack of sensitivity is, probably, the absence of large scale thermal advection within the Tropics, as pointed out by Ref. Bristow & Campbell [8]. Chen et al. [24] noticed that model 1 gives better estimates in tropical rather than in extratropical latitudes, where maximum and minimum temperatures are largely determined by temperature advection. However, the values of the coefficients are quite different from those found by Ref. Liu X et al. [19] for the Haerbin province in China, a fact that reinforces the need of calibration with local data. Coefficient  $\beta_2$  of models 1 and 3 did not exhibit any clear pattern for the different regions of this study, but the other two coefficients ( $\beta_1$  and  $\beta_3$ ) showed a linear dependence with respect to latitude and longitude (Fig. 2).

Table 2  
Models used in this work.

Model identification number	Model	Coefficients	Authors
1	$H_g/H_o = \beta_1[1 - \exp(-\beta_2\Delta T^{\beta_3})]$	$\beta_1, \beta_2$ and $\beta_3$	[8]
2	$H_g/H_o = 0.75[1 - \exp(-\beta_2\Delta T^2)]$	$\beta_2$	[9]
3	$H_g/H_o = \beta_1[1 - \exp(-\beta_2\Delta T^{\beta_3}/\Delta T_m)]$	$\beta_1, \beta_2$ and $\beta_3$	[10]
4	$H_g/H_o = 0.75[1 - \exp(-\beta_2\Delta T^2/H_o^{\beta_3})]$	$\beta_2$	[11]
5	$H_g/H_o = 0.75[1 - \exp(-\beta_2\Delta T^2/\Delta T_m)]$	$\beta_2$	[12]
6	$H_g/H_o = \beta_1(\Delta T)^{\frac{1}{2}}$	$\beta_1$	[13]
7	$H_g/H_o = \beta_1(1 + 2.7 \times 10^{-5} \times \text{Altitude})(\Delta T)^{\frac{1}{2}}$	$\beta_1$	[14]
8	$H_g/H_o = \beta_1$ and $\beta_2$	$\beta_1$ and $\beta_2$	[16]
9	$H_g/H_o = (\beta_1(\Delta T)^{\frac{1}{2}} + \beta_2)$ $H_g/H_o = \beta_1(\Delta T)^{\frac{1}{2}} + \beta_2/H_o$	$\beta_1$ and $\beta_2$	[17]

$\Delta T$  = thermal amplitude ( $^{\circ}\text{C}$ );  $\Delta T_m$  = monthly average of  $\Delta T$  ( $^{\circ}\text{C}$ ),  $H_g$  = daily global solar irradiation ( $\text{MJ m}^{-2}$ ) and  $H_o$  = daily global solar irradiation at the top of the atmosphere ( $\text{MJ m}^{-2}$ ).

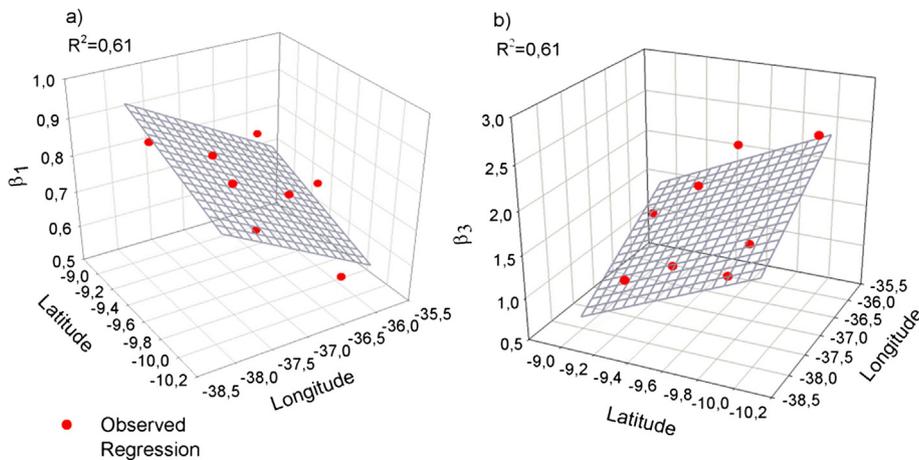
**Table 3**  
Daily coefficients of the models, using  $\Delta T_1$  (in models 6, 7, 8 and 9) and  $\Delta T_2$  (in models 1, 2, 3, 4 and 5).

Site	Água Branca			Pão de Açúcar		
Model/coeff.	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_1$	$\beta_2$	$\beta_3$
1	0.887*	0.078*	1.164*	0.844*	0.091*	1.207*
2	–	0.019*	–	–	0.018*	–
3	0.887*	0.719*	1.164*	0.844*	0.949*	1.207*
4	–	0.635*	–	–	0.603*	–
5	–	0.173*	–	–	0.186*	–
6	0.187*	–	–	0.191*	–	–
7	0.184*	–	–	0.191*	–	–
8	0.248*	–0.188*	–	0.223*	–0.103*	–
9	0.218*	–3.371*	–	0.199*	–0.899*	–
Site	Santana do Ipanema			Palmeira dos Índios		
Model/coeff.	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_1$	$\beta_2$	$\beta_3$
1	0.838*	0.080*	1.096*	0.604*	0.085*	1.861*
2	–	0.012*	–	–	0.021*	–
3	0.838*	0.954*	1.096*	0.604*	0.700*	1.861*
4	–	0.405*	–	–	0.613*	–
5	–	0.145*	–	–	0.185*	–
6	0.168*	–	–	0.186*	–	–
7	0.167*	–	–	0.184*	–	–
8	0.196*	–0.098*	–	0.187*	–0.003*	–
9	0.176*	–0.936*	–	0.174*	–1.257*	–
Site	Arapiraca			Maceió		
Model/coeff.	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_1$	$\beta_2$	$\beta_3$
1	0.762*	0.103*	1.248*	0.707*	0.033*	2.113*
2	–	0.018*	–	–	0.024*	–
3	0.762*	0.906*	1.248*	0.707*	0.259*	2.113*
4	–	0.632*	–	–	0.811*	–
5	–	0.162*	–	–	0.185*	–
6	0.185*	–	–	0.201*	–	–
7	0.184*	–	–	0.200*	–	–
8	0.222*	–0.111*	–	0.307*	–0.300*	–
9	0.199*	–1.421*	–	0.255*	–5.302*	–
Site	Coruripe			São José da Laje		
Model/coeff.	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_1$	$\beta_2$	$\beta_3$
1	0.580*	0.018**	2.517*	0.771*	0.082*	1.171*
2	–	0.018*	–	–	0.012*	–
3	0.580*	0.163**	2.517*	0.771*	0.810*	1.171*
4	–	0.611*	–	–	0.420*	–
5	–	0.162*	–	–	0.119*	–
6	0.178*	–	–	0.160*	–	–
7	0.178*	–	–	0.159*	–	–
8	0.140*	–0.116*	–	0.206*	–0.147*	–
9	0.148*	–3.144*	–	0.180*	–2.214*	–

\*Significant to 95% confidence interval. \*\*Non significant.

The determination coefficient ( $R^2$ ) was 0.61 for the multiple linear regression model with an adjustment between  $\beta_1$  and  $\beta_3$  (dependent variables) and the geographic coordinates (independent variables). This indicates that the latitudinal and longitudinal variation explain most of the variability of these coefficients. The coefficient  $\beta_2$  in models 1 and 3 did not show any statistical significance in their adjustment ( $p < 0.05$ ) with respect to the geographical coordinates. Coefficient  $\beta_2$  was more sensitive than the other two regarding the air temperature schemes. Coefficient  $\beta_1$  changed from 0.580 to 0.887, with the largest values observed in the sites farther from the coastline and coefficient  $\beta_3$  remained within the closed interval [1.096; 2.517] while increasing linearly inland. Coefficient  $\beta_1$  increases linearly northward and westward (inland), while the pattern of  $\beta_3$  was just the opposite (increasing southward and eastward). Coefficient  $\beta_1$  in model 1 (Bristow and Campbell's original model) gives the upper asymptote of the  $H_g/H_o$  curve (maximum value for the transmissivity) and, therefore, is associated with the atmospheric transmissivity of clear sky (which is a function of the local atmospheric composition).  $\beta_2$  and  $\beta_3$  are shape factors which define the rate that  $\beta_1$  is attained as a function of the thermal amplitude; they may be considered an energy partition between sensible and latent heat forms which depend on the climate type and seasonality (dry and rainy periods) [8]. Under clear sky conditions, oxygen, ozone and water vapor are mainly responsible for the attenuation of the solar radiation which is weakly dependent of the optical depth due to the relatively low topography of the region [40,41]. Other gases as well aerosols and pollutants contribute in a less extent to the attenuation of solar energy. Transmissivity is also affected by altitude.

The distance from the coastline, associated with a decrease in the total precipitation, creates a zonal gradient of humidity with the most humid areas being the coastal region, lower São Francisco River and the humid zone; the driest being the semi-arid hinterland and upper São Francisco basin and the hinterlands being the transition zone. Agua Branca is an isolated exception to this pattern due to the local topography what explains why the site is more humid than its surroundings. This atmospheric water content gradient is well established during summer (also the dry season), when the maximum values of transmissivity are expected. As  $\beta_1$  is an indirect measure of the clear sky transmissivity and also due to the selective water vapor attenuation bands, one may find the smallest values of this coefficient (corresponding to the largest attenuation) near the coastal zone and gradually larger values toward the dry interior. Another reason to explain the behavior of this coefficient is the topography with higher values away from the coastline. The meridional changes in  $\beta_1$  (increase northward) is



**Fig. 2.** Relation between the coefficients a)  $\beta_1$  and b)  $\beta_2$  of the Bristow–Campbell model (model 1) for the global daily solar radiation and the latitude and longitude.

associated with the large topography gradient in this direction, with the lower regions located to the south, close to São Francisco Valley (<50 m) and the highest regions in the neighborhood of Borborema Mase (up to 650 m). As the altitude increases, the optical depth decreases and transmissivity increases [15]. The larger (smaller)  $\beta_3$  the smaller (larger) are the thermal amplitudes and their variations in order to reach maximum values of transmissivity. Therefore regions close to the coast, show larger values of  $\beta_3$  as expected due, to the smaller thermal amplitude brought about by lack of continentality. As a result,  $\beta_3$  tend to decrease westward. This decrease is also due to topographic change, which also increases westward and favors an increase in the thermal amplitude. The north-south change pattern of  $\beta_3$  (northward decrease) is explained by the topographic features already cited.

The coefficients  $\beta_2$  of models 3 and 1 were one order of magnitude different and coefficients  $\beta_1$  and  $\beta_3$  of model 3 did not differ significantly from those of model 1, for all sites considered in this study. The coefficients  $\beta_2$  of models 2, 4 and 5 were all different among the sites; their values were between 0.012 and 0.024 (model 2), 0.405 and 0.811 (model 4), and 0.119 and 0.186 (model 5). The constant values of  $\beta_1$  and  $\beta_3$  in models 2, 4 and 5 resulted in large differences for the adjusted value of  $\beta_2$ ; these differences were not observed in models 1 and 3, both with  $\beta_1$  and  $\beta_3$  adjusted before for the climatic conditions in Alagoas State. In general, the differences among the three coefficients were quite small, for both air temperature schemes. Concerning models 1 and 3, their coefficients  $\beta_1$  (Arapiraca and São José da Laje) and coefficient  $\beta_3$  (for Maceió and Coruripe) were very close to the corresponding coefficients of models 2 and 5 ( $\beta_1 = 0.75$  and  $\beta_3 = 2$ ).

The values of all coefficients, for all sites used in this study were different from those of Bristow & Campbell [8] with variations of 0.580–0.887 (for  $\beta_1$ ) and 0.018 to 0.103 (for  $\beta_2$ ); the coefficient  $\beta_3$  changed from 1.196 to 2.517. Meza & Varas [9] used  $\beta_1 = 0.70$  and  $\beta_3 = 2.4$  and adjusted the remaining coefficient for 21 sites in Chile. They found that  $\beta_2$  changes from 0.0015 to 0.0194, values different from those of Goodin et al. [25] and Weiss et al. [11], and also from those obtained in this study with local calibrations. For model 6, Annandale et al. [14], Allen et al. [26] and Hargreaves & Samani [13] proposed fixed values of  $\beta_1 = 0.16$  (inland) and  $\beta_1 = 0.19$  (coastal regions). For the coastal sites of Maceió and Coruripe, the differences among the proposed values of coefficient  $\beta_1$  were 5.5% lower than those of the adjusted values. However, the agreement was good for Pão de Açúcar, a site located in the interior region but at the margin of

São Francisco River. The values of coefficient  $\beta_1$  in this study changed from 0.160 to 0.201, depending on the model (6 or 7) and the region. This range was different from that found by Ref. Liu X et al. [19] (0.135–0.166), for the Haerbin province in China. Ball et al. [27] also noticed a large variation of 0.130–0.170 for 13 sites in USA; again, these differences reinforce the need of adjustment with local data. The coefficients  $\beta_1$  of models 6 and 7 were not very different from each other, probably due to the smooth topography of the region.

Within the range of altitudes of the sites used in this study, the differences between altitude-corrected and non-corrected values of  $\beta_1$  in model 7 were less than 1.6%. Coefficients  $\beta_1$  of models 6 and 7 also showed a strong dependence on the geographical coordinates with  $R^2 = 0.86$  (Fig. 3), decreasing from the coastal region inland (~36.96° W), and then, increasing toward the westernmost part of Alagoas State. Regarding latitudinal changes, the values increased from south to the central part of the State (~9.66° S) followed by a northward decrease. The calculation of  $\beta_1$  for models 6, 7, 8 and 9 was almost independent of the temperature schemes, even for models 6 and 7 which had the altitude correction included.

**Table 4**

Averaged daily monthly coefficients of models using  $\Delta T_1$  (models 6, 7, 8 and 9) and  $\Delta T_2$  (models 1, 2, 3, 4 and 5).

Site	Água Branca			Pão de Açúcar		
	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_1$	$\beta_2$	$\beta_3$
Model/coeff.						
1	0.654*	0.049**	1.706*	0.684*	0.041**	1.769*
2	–	0.019*	–	–	0.017**	–
3	0.654*	0.451**	1.706*	0.684*	0.381**	1.769*
4	–	0.632*	–	–	0.566*	–
5	–	0.173*	–	–	0.177*	–
6	0.185*	–	–	0.190*	–	–
7	0.182*	–	–	0.190*	–	–
8	0.190*	–0.013**	–	0.181*	–0.030**	–
9	0.191*	–0.611*	–	0.184*	–0.676*	–

Site	Santana do Ipanema			Palmeira dos Índios		
	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_1$	$\beta_2$	$\beta_3$
Model/coeff.						
1	0.721*	0.012**	1.078**	0.571*	0.003**	1.465**
2	–	0.012**	–	–	0.020*	–
3	0.721*	0.110**	1.078**	0.571*	0.115**	1.465**
4	–	0.392*	–	–	0.689*	–
5	–	0.141*	–	–	0.170*	–
6	0.167*	–	–	0.187*	–	–
7	0.165*	–	–	0.185*	–	–
8	0.143*	–0.083**	–	0.120**	–0.194**	–
9	0.155*	–1.377*	–	0.158**	–2.938*	–

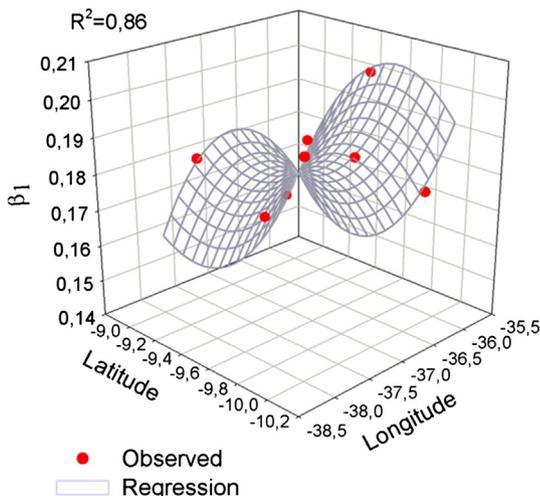
  

Site	Arapiraca			Maceió		
	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_1$	$\beta_2$	$\beta_3$
Model/coeff.						
1	0.728**	0.013**	1.065**	0.720*	0.034**	1.841**
2	–	0.018*	–	–	0.023*	–
3	0.728**	0.130**	1.065**	0.720*	0.267**	1.841**
4	–	0.604*	–	–	0.781*	–
5	–	0.155*	–	–	0.177*	–
6	0.184*	–	–	0.199*	–	–
7	0.183*	–	–	0.198*	–	–
8	0.183*	–0.003**	–	0.315*	–0.324*	–
9	0.186*	–0.216*	–	0.240*	–3.973*	–

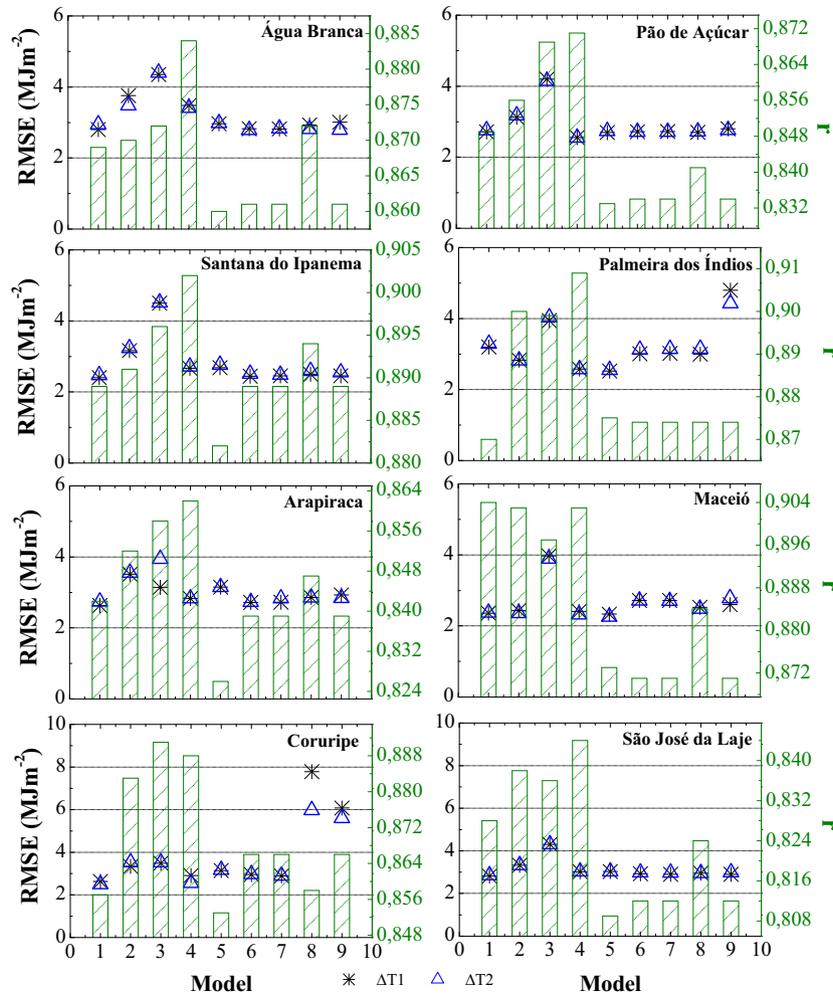
  

Site	Coruripe			São José da Laje		
	$\beta_1$	$\beta_2$	$\beta_3$	$\beta_1$	$\beta_2$	$\beta_3$
Model/coeff.						
1	0.557*	0.060**	1.891**	2.700**	0.050**	0.61*
2	–	0.017*	–	–	0.012*	–
3	0.557*	0.543**	1.891**	2.700**	0.883**	0.61*
4	–	0.587*	–	–	0.411*	–
5	–	0.155*	–	–	0.116*	–
6	0.178*	–	–	0.158*	–	–
7	0.178*	–	–	0.157*	–	–
8	0.062**	–0.350*	–	0.175*	–0.053**	–
9	0.132*	–4.822*	–	0.162*	–0.470*	–

\*Significant to 95% confidence interval. \*\*Non significant.



**Fig. 3.** Relation between the coefficient  $\beta_1$  of Hargreaves & Samani model (model 6) for the global daily solar radiation and the latitude and longitude.



**Fig. 4.** Root mean square error (RMSE) based on the two air temperature schemes ( $\Delta T_1$  and  $\Delta T_2$ ) and the correlation coefficient ( $r$ ) using  $\Delta T_1$  (models 6, 7, 8 and 9) and  $\Delta T_2$  (models 1, 2, 3, 4 and 5).

Changes in  $\beta_1$  are expected for models 6 and 7 in order to satisfy the relation between  $H_g/H_o$  and the  $\Delta T^{0.5}$  [15]. Furthermore, larger values of  $\beta_1$  are expected for coastal regions or near large bodies of water or humid regions (where the temperature amplitude is reduced by either land/sea contrast or atmospheric humidity). Inversely, smaller values of this coefficient are expected in dry regions or sufficiently away from moisture sources [15,28]. Under these conditions, the increase (decrease) in humidity implies smaller (larger) thermal amplitudes.  $\beta_1$  coefficient of model 6 (Hargreaves & Samani) tends to be larger (smaller) than those of the other models in order to compensate for the effects of smaller (larger) thermal amplitudes.

**Table 5**  
Performance of the models with the best estimations of the daily global solar irradiation for each site and their statistical indicators [root mean square error (RMSE) and correlation coefficient ( $r$ )].

Daily global solar irradiation			
Site	Model	RMSE (MJ m <sup>-2</sup> )	$r$
Água Branca	6 and 7	2.821	0.861
Pão de Açúcar	8	2.701	0.841
Santana do Ipanema	6 and 7	2.452	0.889
Palmeira dos Índios	4	2.574	0.909
Arapiraca	6 and 7	2.722	0.839
Maceió	1	2.372	0.904
Coruripe	1	2.498	0.857
São José da Laje	1	2.846	0.828

This pattern is present in this work, as shown by a regression analyses between  $\beta_1$  and the geographical coordinates given in Fig. 3. A pattern of zonal change was noted at the sites near the coast and westernmost region of Alagoas (the humid region of Água Branca) with the largest values of  $\beta_1$ ; the smallest values are found in the central part of the state (subhumid and semiarid). Regarding the meridional variations, the largest values of  $\beta_1$  occurs near the central northern part of the state (more humid) and decreasing northward and southward (drier regions). Due to the nonlinear relation between  $H_g/H_o$  and  $\Delta T^{0.5}$ ,  $\beta_1$  did not show any linear trend, as noticed for the coefficients of model 1 (Bristow & Campbell model).

Coefficients  $\beta_2$  of models 8 and 9 were more sensitive to the  $\Delta T$  schemes than the corresponding coefficients  $\beta_1$ . In addition, coefficients  $\beta_2$  of these models were larger, in absolute values, when the  $\Delta T_1$  scheme was used. One also notices that coefficients  $\beta_1$  of model 8 for all sites (but Coruripe) were larger than those of model 9. Coefficients  $\beta_2$  of these models for all sites were negative with a large dispersion regarding the geographical positions. These results were all similar to those of Chen et al. [24] who obtained (for model 8)  $\beta_1$  changing from 0.140 to 0.307 (average 0.193) and  $\beta_2$  changing from  $-0.003$  to  $-0.300$  (average 0.130). As the model adjustment is not much affected by the choice of the air temperature scheme, the estimates of the global solar irradiation are discussed in this study using the results of Hargreaves & Samani model (and its modified versions) with the  $\Delta T_1$  scheme and Bristow & Campbell model (and its adaptations) using the  $\Delta T_2$  scheme.

**Table 6**

Performance of the models with the best estimations of the daily global solar irradiation for each region and their statistical indicators [root mean square error (*RMSE*) and correlation coefficient (*r*)].

Daily global solar irradiation			
Region	Model	<i>RMSE</i> ( $\text{MJ m}^{-2}$ )	<i>r</i>
Interior (Sertão)	6 and 7	2.665	0.864
Hinterland (Agreste)	6 and 7	2.867	0.852
Humidity area (Coastal Zone) Zona da Mata/Litoral	1	2.572	0.863

### 3.2. Coefficients for the daily monthly averaged global solar irradiation ( $H_g^m$ )

The coefficients for  $H_g^m$  are shown in Table 4. In general, they appear to be not very sensitive to the choice of the air temperature scheme, although the model of Bristow & Campbell and its modified versions show conspicuous differences for some sites. Therefore, the discrepancy among the coefficients is not statistically significant with  $\beta_1$  and  $\beta_2$  decreasing and  $\beta_3$  increasing. No regional pattern for the coefficients was noticed for the interior, hinterlands and humid/coastal zones. São José da Laje showed the largest value of  $\beta_1$  (2.700). The coefficients  $\beta_2$  and  $\beta_3$  of these models at Palmeira dos Índios were 0.003 and 1.465, respectively. An appreciable difference in the values of  $\beta_2$  (model 4), regarding the temperature scheme, was noticed only for Água Branca (in the interior and with a higher altitude) namely  $\beta_2 = 0.632$  (using the  $\Delta T_2$  scheme) and  $\beta_2 = 0.173$  (using the  $\Delta T_1$  scheme); this difference may be attributed to topographic effects. Meza & Varas [9] noticed that model 1 is more appropriated to estimate daily values and, practically useless, to obtain monthly averages by extrapolation.

Coefficients  $\beta_1$  of model 6 did not show any pattern for any site; São José da Laje (humid zone but hilly) had the smallest value (0.158) and Maceió (coastal zone but flat terrain), the largest 0.199. An analysis of the coefficients  $\beta_1$  of models 6 and 7 showed that they are independent of the temperature scheme (practically the same values were obtained) what means that the altitude correction used in model 7 did not bring any improvement. On the other

hand, the coefficients  $\beta_1$  and  $\beta_2$  of models 8 and 9 showed some, but not strong, dependence with respect to the air temperature scheme, with the largest value of  $\beta_1 = 0.315$  (model 8 at Maceió). As observed for the daily estimates, the choice of the temperature scheme does not affect significantly the results on a monthly scale. The ensuing results are still based on the calibration of Hargreaves & Samani model (and its modifications) using the  $\Delta T_1$  scheme and Bristow & Campbell model (and its adaptations) with the  $\Delta T_2$  scheme.

### 3.3. Estimates of the daily global solar irradiation ( $H_g^d$ )

The *RMSE* values (Fig. 4) show that the results do not depend much on the temperature schemes except for Arapiraca (model 4) and Coruripe (models 2, 5 and 8). The same results were independent of the site altitude, what apparently seems to be contrary to the results of Liu X et al. [19]. This seemingly contradiction can be explained recalling that the topographic features of the stations in China (ranging from 3 to 2295 m, as shown by the authors) and Alagoas State (30 m at Pão de Açúcar and 593 m at Água Branca) are quite different; the maximum altitude in Alagoas is only 26% of that in China. The smallest *RMSE* values for the interior sites were found at Santana do Ipanema, quite close to the values found for Água Branca and Pão de Açúcar. The *RMSE* indices obtained with the  $\Delta T_1$  scheme were consistently smaller than those using the  $\Delta T_2$  scheme at Arapiraca, São José da Laje and Santana de Ipanema for all models. The average for all sites using the  $\Delta T_1$  scheme ( $3.08 \text{ MJ m}^{-2}$ ) was 0.55% smaller than the corresponding one with the  $\Delta T_2$  scheme ( $3.10 \text{ MJ m}^{-2}$ ). The average *RMSE* for all sites in the interior (Água Branca, Pão de Açúcar and Santana do Ipanema), using models 2, 4 and 5 was  $3.00 \text{ MJ m}^{-2}$  and  $2.91 \text{ MJ m}^{-2}$  for the hinterlands sites (Arapiraca and Palmeira dos Índios), with models 2, 4 and 5. This shows that the use of different temperature schemes does not change significantly the results and therefore most of the models are capable of estimating  $H_g^d$  quite satisfactorily for all the sites in Alagoas State. In practice, fixing the coefficients in the initial calibration stages makes the model performance significantly worse (see Models 2, 4 and 5, in particular, for the interior sites). The use of models with only one coefficient (models 2,4,5, 6 and 7) yielded larger errors at São José da Laje and Água Branca both located in hilly terrain; this error was relatively larger at Maceió and Coruripe (coastal and plain sites). These results are quite similar to those found for 64 stations in Iran [36] with an average *RMSE* of  $2.80 \text{ MJ m}^{-2}$  and evidenced the possibility of overestimation during warm periods or underestimation during cold periods.

The changes introduced in model 1 were not efficient and did not produce any improvement in the estimates. The performance of model 2 (variation of Bristow & Campbell's model, with pre fixed values of  $\beta_1 = 0.75$  and  $\beta_3 = 2$ ) was worse than that of models 4 and 5, for most of the sites in this study. Model 4 had a better performance than that of model 1 just at Palmeira dos Índios. For this reason, the original model of Bristow & Campbell (model 1) is preferred rather than their modified version. This statement agrees with that of Liu X et al. [19] in which model 1 had a much better performance than the modified version [9–12,25].

The principal results on the performance of the models in estimating the daily global solar irradiation are given in Table 5, showing the most suitable models for each one of the sites of this study, according to their statistical indicators (*RMSE* and correlation coefficient). Model 1 was more accurate than model 6 for Maceió, Coruripe (both within the coastal zone) and São José da Laje (in the humid area) and yielded similar results to those of Supit & Kappel [29] for some sites in Europe. Models 6 and 7 show better performance than that of model 1 for Água Branca and Santana do Ipanema (in the interior) and Arapiraca (in the hinterlands); models 8

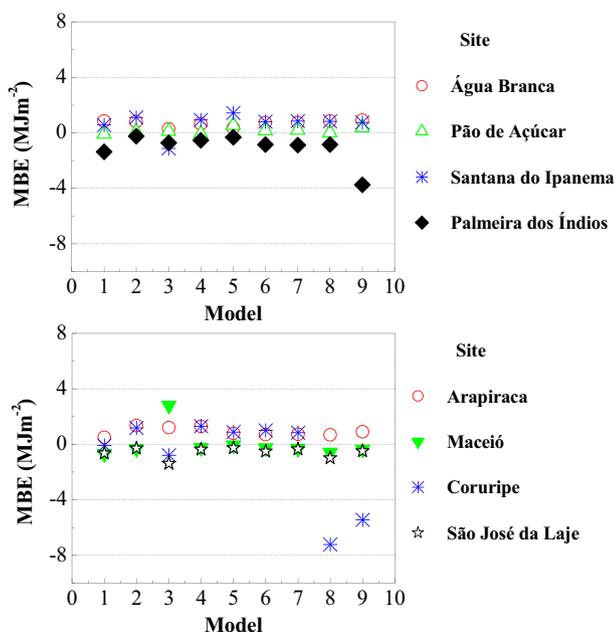


Fig. 5. Mean bias error (*MBE*) for the models and stations, using the temperature schemes  $\Delta T_1$  (models 6, 7, 8 and 9) and  $\Delta T_2$  (models 1, 2, 3, 4 and 5).

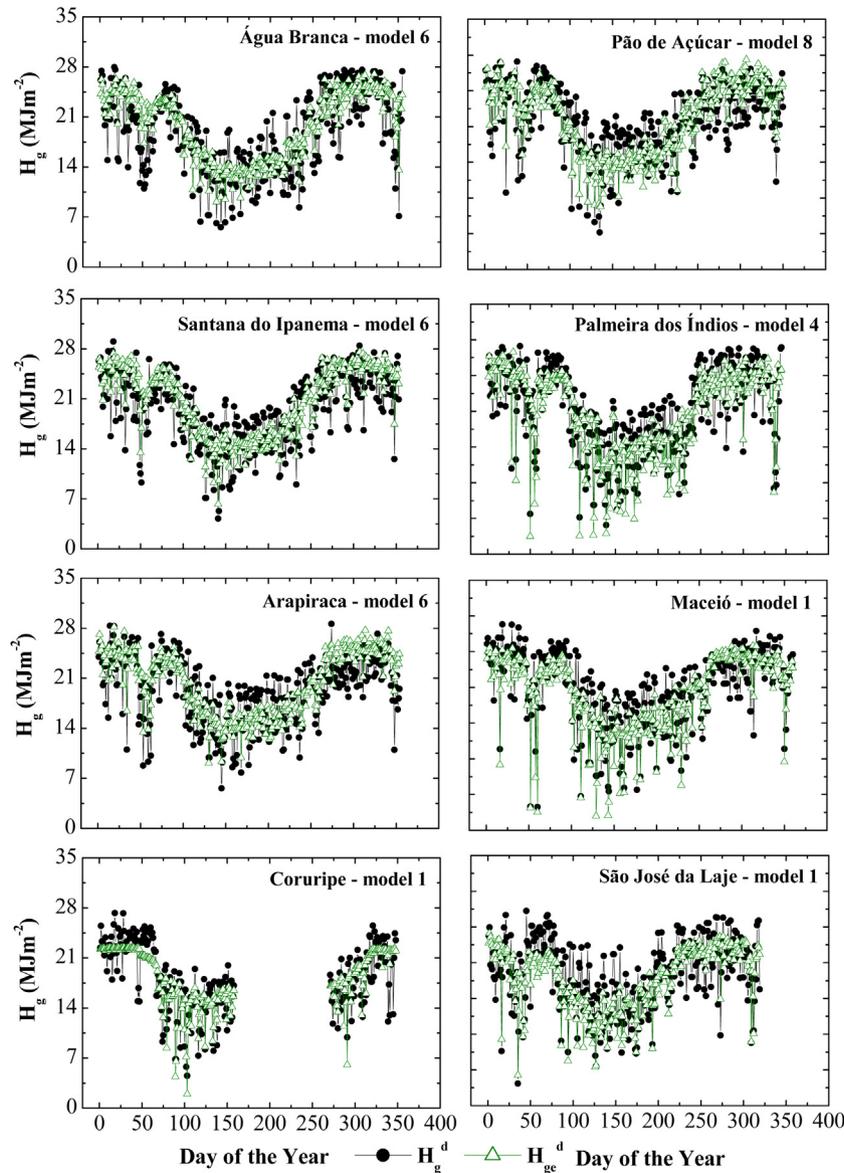


Fig. 6. Daily observed ( $H_g^d$ ) and estimated ( $H_{ge}^d$ ) variations of the global solar irradiation for some stations in Alagoas State 2009.

and 4 are considered the most adequate for Pão de Açúcar and Palmeira dos Índios, respectively. Bandyopadhyay et al. [30] found the original model 6 and the one adapted by Allen et al. [26] more accurate in estimating the crop evapotranspiration for some regions in India. The FAO-56 Bulletin recommends the use of the model adapted by Allen et al. [26], when  $H_g$  data are missing or dubious. Considering the local results, the RMSE values are similar or even better than those found by Linares-Rodríguez et al. [37] for Andaluza, Spain (RMSE between 2.83 and 3.01 MJ m<sup>-2</sup>) obtained with an artificial neural network.

Table 6 summarizes the results on the models' performance in a regional context. Model 1 is the one that produced the best estimates for all the sites located in the humid and northern coastal areas; models 6 and 7 are considered more appropriate for the interior and hinterlands. Allen [15] obtained similar results with model 6 (Hargreaves & Samani model) yielding better estimates of  $H_g$  for the sites in the interior rather than the coastal ones. In the present study, a large variability in the coastal cloud coverage was noticed due to the prevailing weather systems (e.g., sea/land

breezes and trade winds) and their interaction with the local topography, what explains the large changes in  $H_g$  [31]. The presence of the ocean produces small temperature amplitude and, since the relationship between  $H_g$  and the thermal amplitude is nonlinear, the combined effect of high variability in  $H_g$  and small temperature amplitudes is likely to produce large dispersion and errors in  $H_g$  [15].

There was a significant difference between the  $H_g^d$  and  $H_{ge}^d$  series (the observed and estimated daily global solar irradiation, respectively) when the  $t$ -test was used, although the statistical parameters (RMSE and  $r$ ) indicated acceptable estimates. In general, the Bristow & Campbell model (model 1) underestimated the daily global solar irradiation in Pão de Açúcar ( $MBE = -0.083$  MJ m<sup>-2</sup>), Palmeira dos Índios ( $MBE = -1.370$  MJ m<sup>-2</sup>), Maceió ( $MBE = -0.681$  MJ m<sup>-2</sup>), Coruripe ( $MBE = -0.090$  MJ m<sup>-2</sup>) and São José da Laje ( $MBE = -0.638$  MJ m<sup>-2</sup>), and overestimated it for the rest of the sites (Fig. 5). Models 2, 4 and 5 showed a trend to overestimate  $H_g^d$  at Água Branca, Arapiraca, Santana do Ipanema and Coruripe and underestimate it at Palmeira dos Índios, Maceió

and São José da Laje. Hargreaves & Samani's [13] model and the modified models 7, 8 and 9 underestimated  $H_g^d$  at Palmeira dos Índios, Maceió and São José da Laje, and overestimated it at Água Branca, Arapiraca and Santana do Ipanema. Overestimates (with models 6 and 7) and underestimates (with models 8 and 9) for the regions of Pão de Açúcar and Santana do Ipanema were also observed.

The observed and estimated annual variations of  $H_g^d$  with the most suitable models for each site are shown in Fig. 6. It can be seen that the largest deviations are associated with large variations in cloudiness, and consequently with the scattering of solar radiation. The irradiation changes throughout the year, with the largest values occurring during the dry period (Spring and Summer) and the smallest ones during the rainy period (Autumn and Winter). The solar declination has a secondary role in contributing to these seasonal differences [31]. The fluctuations observed in January and February were brought about by the heavy episodes of precipitation in the entire Alagoas State, with totals of 244.3 mm (Coruripe, southern coastal zone) and 75.2 mm (Arapiraca, hinterland).

3.4. Estimates of the monthly daily averaged global solar irradiation ( $H_g^m$ )

Good estimates of  $H_g^m$  were obtained using all models for all sites stud (Fig. 7), with models 1 and 6 leading the list. The worst estimates came from models 3 and 8 which consistently showed high RMSE values for Santana do Ipanema, Arapiraca, Palmeira dos Índios and São José da Laje. The initial calibration of these models did not improve their overall performances. The model of

Hargreaves & Samani [13] and the one modified by Annadale et al. [14] showed similar statistical indicators implying that the altitude correction is not needed for these sites, in agreement with Liu X et al. [19]. Models 8 and 9 (adaptations of model 6) had a poorer performance when compared to that of model 6; model 8 yielded RMSE values of  $14.53 \text{ MJ m}^{-2}$  (Palmeira dos Índios) and  $25.11 \text{ MJ m}^{-2}$  (Coruripe). However, the correlation coefficients obtained with different models at Água Branca varied from 0.932 to 0.954 with the best estimated value of  $H_g^m$  given by model 8 (RMSE =  $1.39 \text{ MJ m}^{-2}$  and  $r = 0.941$ ). Therefore, the statistical indicators show that both models 8 and 9 had similar good performance em Água Branca, Arapiraca, Maceió e São José da Laje. This was confirmed by the *t*-test which did not detect any significant differences between model estimates and measurements. However, these indicators did show that model 1 yielded the best estimates of  $H_g^m$  at Pão de Açúcar (RMSE =  $1.47 \text{ MJ m}^{-2}$ ), Santana do Ipanema (RMSE =  $1.12 \text{ MJ m}^{-2}$ ), Arapiraca (RMSE =  $1.39 \text{ MJ m}^{-2}$ ) and Coruripe (RMSE =  $1.63 \text{ MJ m}^{-2}$ ). These results were also consistent with the correlation (*r*) between the estimates and observations (all in the closed interval [0.919, 0.987]). In particular, RMSE =  $1.95 \text{ MJ m}^{-2}$  (model 4) and RMSE =  $1.25 \text{ MJ m}^{-2}$  (model 6) were obtained at Palmeira dos Índios. These errors are smaller than those of Eskisehir (RMSE between 3.640 and  $3.711 \text{ MJ m}^{-2}$ , *r* between 0.817 and 0.824 and MBE between  $-3.541$  and  $-3.434$ ), but equal or larger than those obtained for sites in Turkey [38], probably due to the different climatic conditions.  $H_g^m$  values at Maceió were better estimated (RMSE =  $0.68 \text{ MJ m}^{-2}$ ,  $r = 0.98$ ) with models 6 and 7. Models 6 and 7 showed small values of RMSE and high values of *r* for Palmeira dos Índios, São José da Laje and Maceió.

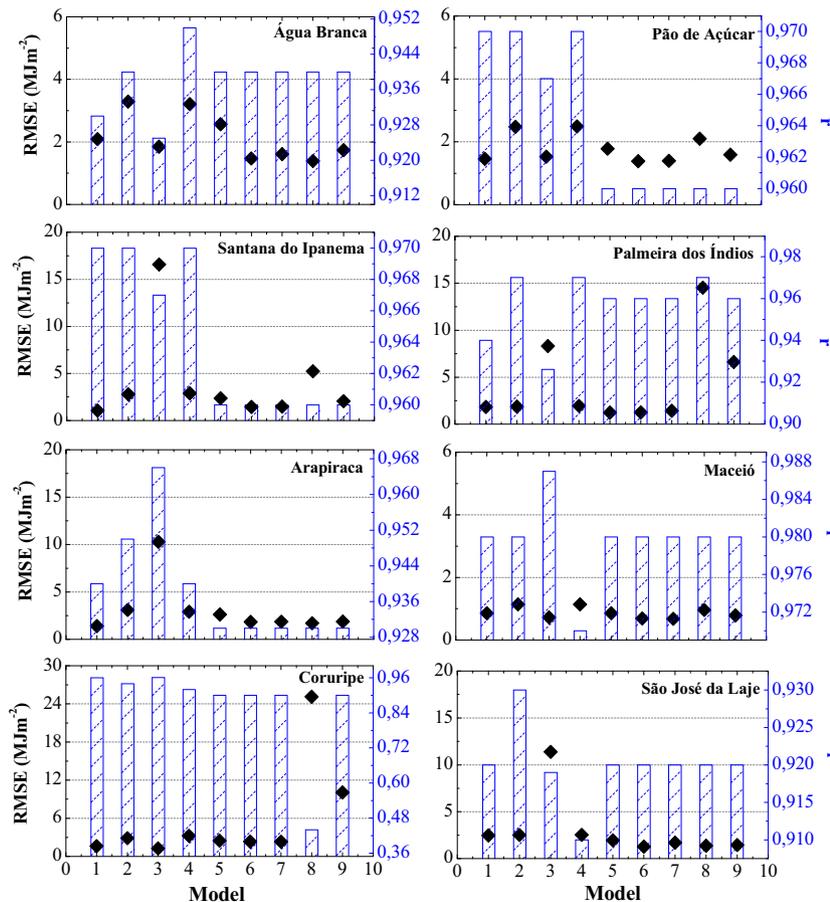


Fig. 7. Root mean square error (RMSE) and the correlation coefficient (*r*) for stations in Alagoas States using models 6, 7, 8 and 9 (with the  $\Delta T_1$  temperature scheme) and models 1, 2, 3, 4 and 5 (with the  $\Delta T_2$  temperature scheme).

The comparison between the results for Alagoas and those in Iran [39] showed that the former ones were larger than those of Karaj (RMSE between 2.16 and 3.16 MJ m<sup>-2</sup>) and Tabriz (RMSE between 2.38 and 2.66 MJ m<sup>-2</sup>), but similar to those of Tehran (RMSE between 1.38 and 1.61 MJ m<sup>-2</sup>), Shiraz (RMSE between 1.03 and 2.10 MJ m<sup>-2</sup>) and Mashhad (RMSE between 0.71 and 1.56 MJ m<sup>-2</sup>). Our results were only smaller than those Isfahan (RMSE between 0.510 and 0.823). The differences above are quite likely due to different climatic conditions and techniques to achieve the best adjustment of the model coefficients.

As seen in Fig. 8, the overall performance of the models was satisfactory for all the sites as evidenced by the low absolute values of MBE. Models using the  $\Delta T_2$  scheme (models 1, 2, 3 4 and 5) resulted: Palmeira dos Índios and Santana do Ipanema (with model 3 greatly underestimating  $H_g^m$ ) Arapiraca (model 3 with a relatively smaller underestimate) and São José da Laje (overestimated by model 2). Models using the  $\Delta T_1$  scheme (models 6, 7, 8 and 9) did not show a satisfactory performance mainly for Coruripe and Palmeira dos Índios (models 8 and 9 greatly underestimating  $H_g^m$ ) and Santana do Ipanema (underestimated by model 8 only). The worst cases of underestimating  $H_g^m$  were observed for Coruripe (MBE = -24.88 MJ m<sup>-2</sup>, model 8) and Santana do Ipanema (MBE = -16.37 MJ m<sup>-2</sup>, model 3).

#### 4. Conclusions

The model coefficients used in this study were insensitive with respect to the selection of the air temperature scheme ( $\Delta T_1$  and  $\Delta T_2$ ). The model performance using the  $\Delta T_2$  scheme does not statistically differ much from that of the models using the  $\Delta T_1$  scheme. The use of the former scheme is easier and recommended. The generated coefficients used to estimate the global solar irradiation are different for all the sites which require that all of them be calibrated with local data.  $\beta_1$  and  $\beta_3$  coefficients of the original Bristow & Campbell's model and  $\beta_1$  of the Hargreaves & Samani's model showed a spatial dependence with respect to the coastal environment, local climate conditions (dry or wet climate) and cloudiness.

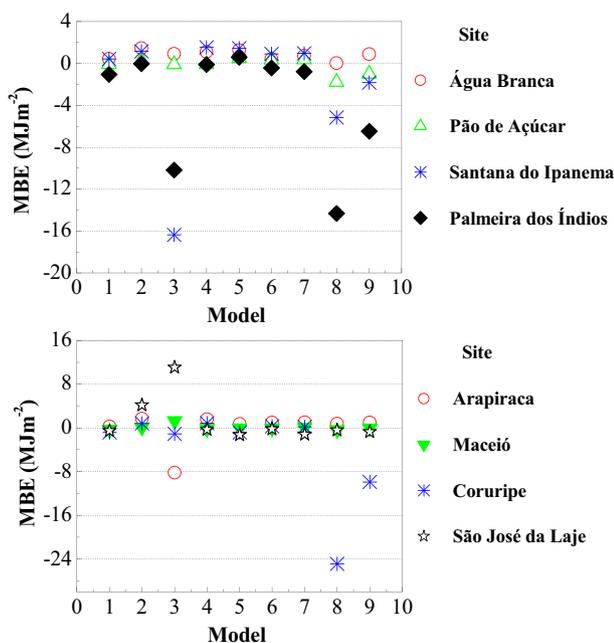


Fig. 8. Mean bias error (MBE, in MJ m<sup>-2</sup>) for all models and for all sites of this study using models 6, 7, 8 and 9 (using the  $\Delta T_1$  temperature scheme) and models 1, 2, 3, 4 and 5 (using the  $\Delta T_2$  temperature scheme).

Simplifications as those used in the Bristow & Campbell model (model 1), by keeping  $\beta_1$  and  $\beta_3$  fixed should be avoided, whenever possible. Model 3 (a modified version of the former) yielded the worst daily and monthly estimates for all of the eight sites. The modified model of Hargreaves & Samani (model 6) produces derived the best estimates of daily  $H_g$  for the stations situated in the hinterlands and interior. The model of Bristow & Campbell was the one with the best performance when applied to the sites within the humid/coastal zones. The original model of Hargreaves & Samani is recommended for the hinterlands and interior and the original Bristow & Campbell for humid/coastal zones, both requiring local calibrations.

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#### References

- [1] El-Sebaei AA, Trabea AA. Estimation of global solar radiation on horizontal surfaces over Egypt. *Egypt J Solids* 2005;28:163–75.
- [2] Almorox J, Hontoria M, Benito M. Models for obtaining daily global solar radiation with measured air temperature data in Madrid (Spain). *Appl Energy* 2011;88:1703–9.
- [3] Spokas K, Forcela F. Estimating hourly incoming solar radiation from limited meteorological data. *Weed Sci* 2006;54:184–9.
- [4] Li H, Ma W, Lian Y, Wang X. Estimating daily global solar radiation by day of year in China. *Appl Energy* 2010;87:3011–7.
- [5] El-Sebaei AA, Al-Hazmi FS, Al-Ghamdi AA, Yaghmour SJ. Global, direct and diffuse solar radiation on horizontal and tilted surfaces in Jeddah, Saudi Arabia. *Appl Energy* 2010;87:568–76.
- [6] Chineke TC. Equations for estimating global solar radiation in data sparse regions. *Renew Energy* 2008;33:827–31.
- [7] Ångström A. Solar and terrestrial radiation. *Quart J R Meteorol Soc* 1924;50:121–6.
- [8] Bristow KL, Campbell GS. On the relationship between incoming solar radiation and daily maximum and minimum temperature. *Agric For Meteorol* 1984;31:159–66.
- [9] Meza F, Varas E. Estimation of mean monthly solar global radiation as a function of temperature. *Agric For Meteorol* 2000;100:231–41.
- [10] Donatelli M, Campbell GS. A simple model to estimate global solar radiation. In: *Proceedings of the 5th European Society of Agronomy Congress*. Nitra, Slovak Republic; 1998. pp. 133–4.
- [11] Weiss A, Hays CJ, Hu Q, Easterling WE. Incorporating bias error in calculating solar irradiance: implications for crop yield simulations. *Agron J* 2001;93:1321–6.
- [12] Abraha MG, Savage MJ. Comparison of estimates of daily solar radiation from air temperature range for application in crop simulations. *Agric For Meteorol* 2008;148:401–16.
- [13] Hargreaves GH, Samani ZA. Estimating potential evapotranspiration. *J Irrig Drain Eng* 1982;108:225–30.
- [14] Annandale JG, Jovanic NZ, Benade N, Allen RG. Software for missing data error analysis of Penman–Monteith reference evapotranspiration. *Irrig Sci* 2002;21:57–67.
- [15] Allen RG. Self-calibrating method for estimating solar radiation from air temperature. *J Hydrol Eng* 1997;2:56–67.
- [16] Hargreaves GL, Hargreaves GH, Riley JP. Irrigation water requirement for Senegal River Basin. *J Irrig Drain Eng* 1985;111:265–75.
- [17] Hunt LA, Kucharb L, Swanton CJ. Estimation of solar radiation for use in crop modeling. *Agric For Meteorol* 1998;91:293–300.
- [18] Paulescu M, Tulcan-Paulescu E, Stefu N. A temperature-based model for global solar irradiance and its application to estimate daily irradiation values. *Int J Energy Res* 2011;35:520–9.
- [19] Liu X, Mei X, Li Y, Wang Q, Jensen JR, Zhang Y, et al. Evaluation of temperature-based global solar radiation models in China. *Agric For Meteorol* 2009;149:1433–46.
- [20] Iqbal M. *An introduction to solar radiation*. New York: Academic Press; 1983.
- [21] Ceballos JC, Rodrigues ML, Oliveira LM. Desempenho do modelo GL versão 1.2 época: Outubro 2010 – Dezembro 2010. Instituto Nacional de Pesquisas Espaciais (INPE), Relatório Técnico 01/11 – Radiação Solar e Terrestre (RST), Divisão de Satélites e Sistemas Ambientais (DSA); 2010 [in Portuguese]. <http://satellite.cptec.inpe.br/radiacao/#/documentos.jsp>.

- [22] Willmott CJ, Matsuura K. Advantages of the mean absolute error (MAE) over the root mean square error (RMSE) in assessing average model performance. *Clim Res* 2005;30:79–82.
- [23] Mostafavi ES, Ramiyani SS, Sarvar R, Moud HI, Mousavi SM. A hybrid computational approach to estimate solar global radiation: an empirical evidence from Iran. *Energy* 2013;49:204–10.
- [24] Chen R, Ersi K, Yang J, Lu S, Zhao W. Validation of five models with measured daily data in China. *Energy Convers Manage* 2004;45:1759–69.
- [25] Goodin DG, Hutchinson JMS, Vanderlip RL, Knapp MC. Estimating solar irradiance for crop modeling using daily air temperature data. *Agron J* 1999;91:845–51.
- [26] Allen RG, Pereira LS, Raes D, Smith M. Crop evapotranspiration—guidelines for computing crop water requirements — FAO. Irrigation And Drainage Paper 56. Rome: Food and Agriculture Organization of the United Nations; 1998. p. 300.
- [27] Ball RA, Purcell LC, Carey SK. Evaluation of solar radiation prediction models in North America. *Agron J* 2004;96:391–7.
- [28] Hargreaves GH. Simplified coefficients for estimating monthly solar radiation in North America and Europe. Utah, EUA: Dept. Biological and Irrigation Engineering, Utah State University; 1994.
- [29] Supit I, Kappel RR. A simple method to estimate global radiation. *Sol Energy* 1998;63(3):147–60.
- [30] Bandyopadhyay A, Bhadra A, Raghuvanshi NS, Singh R. Estimation of monthly solar radiation from measured air temperature extremes. *Agric For Meteorol* 2008;48:1707–18.
- [31] Souza JC, Nicácio RM, Moura MAL. Global solar radiation measurements in Maceió, Brazil. *Renew Energy* 2005;30:1203–20.
- [32] Munner T, Gul M, Kambezidis H. Evaluation of an all-sky meteorological radiation model against long-term measured hourly data. *Energy Convers Manage* 1998;39:303–17.
- [33] Moradi I. Quality control of global solar radiation using sunshine duration hours. *Energy* 2009;34:1–6.
- [34] Jiang Y. Computation of monthly mean daily global radiation in China using artificial neural networks and comparison with other empirical model. *Energy* 2009;34:1276.
- [35] Katiyar AK, Pandey CK. Simple correlation for estimating the global solar radiation on horizontal surfaces in India. *Energy* 2010;35:5043–8.
- [36] Sabziparvor AA, Shetall H. Estimation of global solar radiation in arid and semi-arid climates of the East and West Iran. *Energy* 2007;32:649–55.
- [37] Linares-Rodríguez A, Ruiz-Arias JA, Pozo-Vázquez D, Tovar-Pescador J. Generation of synthetic daily global solar radiation data based on ERA-Interim reanalysis and artificial neural networks. *Energy* 2011;36:5356–65.
- [38] Bakirci K. Correlation for estimation of daily global solar radiation with hours of bright sunshine in Turkey. *Energy* 2009;34:485–501.
- [39] Khorasanizadeh H, Mohammadi K. Introducing the best model for predicting the monthly mean global solar radiation over six major cities of Iran. *Energy* 2013;51:257–66.
- [40] Trabelsi A, Masmoudi M. An investigation of atmospheric turbidity over Kerkennah Island in Tunisia. *Atmos Res* 2011;101:22–30.
- [41] Chaâbane M, Masmoudi M, Medhioub K. Determination of Linke turbidity factor from solar radiation measurement in northern Tunisia. *Renew Energy* 2004;29:2065–76.